## **Neutral Transport Simulations of Gas Puff Imaging Experiments on Alcator C-Mod**

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Note: This poster is available on the Web at: http://w3.pppl.gov/degas2/

#### INTRODUCTION

- Tokamak edge ideal for comprehensive study of turbulence,
  - Accessible with probes
    - $\Rightarrow$  directly measure  $n_e$ ,  $T_e$ , and other properties.
  - Relatively low  $T_e$  facilitates use of atomic physics as basis for diagnostics.
  - Potential payoff great because edge sets boundary conditions for core transport,
    - \* E.g., internal transport barriers, H-mode pedestal.
- Gas Puff Imaging (GPI) experiments designed to measure 2-D structure of edge turbulence,
  - Compare with 3-D nonlinear simulations.
  - And with turbulence measured by probes,
  - Puff neutral gas (e.g., D<sub>2</sub>) near outer wall,
    - View with fast, high res. camera light from electron impact excitation of gas,
    - \* Use sightline  $\parallel \vec{B}$  to see radial & poloidal structure,
- Explore relation between images & plasma fluctuations with DEGAS 2 neutral transport code,
  - Straightforward because puff does not perturb plasma,
  - Emitted light brighter than background,
  - Material surface interactions should not be important.
- Experimental presentation: O-02 J. L. Terry et al.



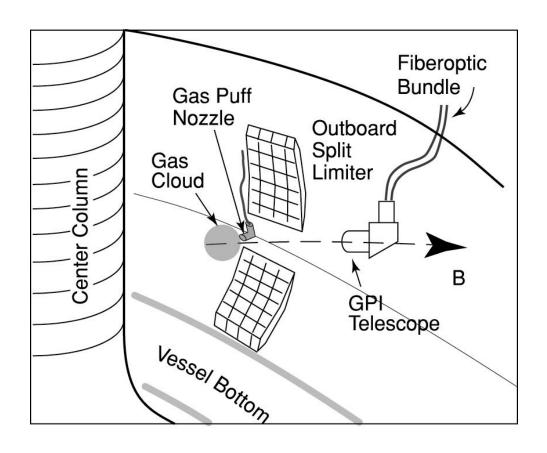
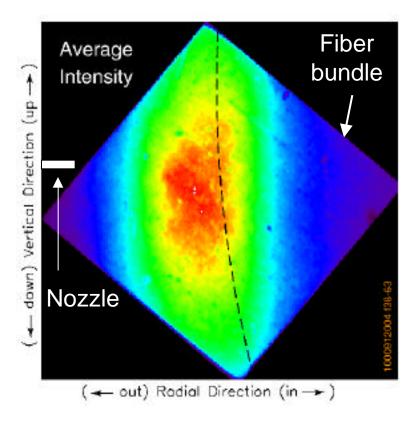


Fig. 1 - Zweben APS '01



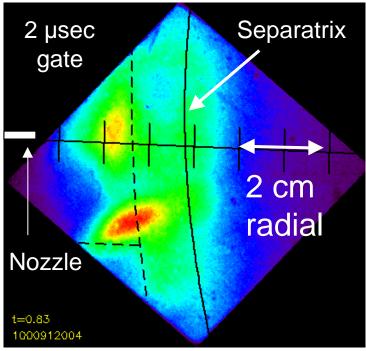


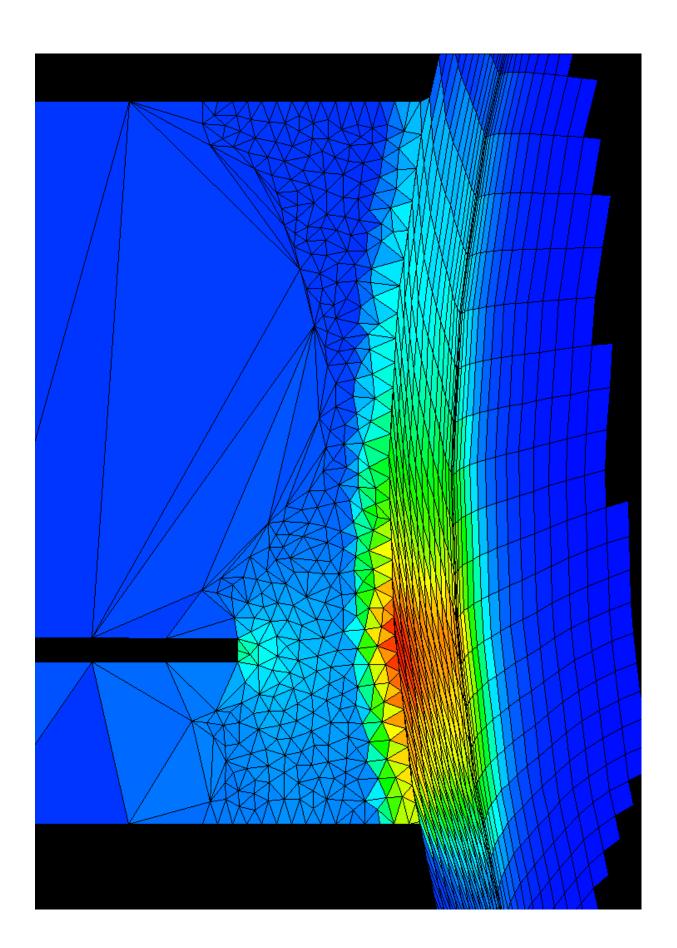
Fig. 2 - Zweben / APS '01

#### **DESCRIPTION OF DEGAS 2 SIMULATIONS**

- Alcator C-Mod Geometry:
  - Start with outline of vacuum vessel,
    - \* Including gas puff nozzle & surrounding structures.
  - EFIT equilibrium for time of interest ⇒
    - \* 2-D plasma mesh set up using DG & Carre,
    - \* Bunch surfaces & grid points to get resolution3 mm or smaller in region of interest.
  - Divide puff region into  $\sim 3$  mm triangles using Triangle.
- Simulations 2-D axisymmetric for now,
  - Output is averaged over toroidal angle.
  - $\Rightarrow$  poloidal plane variation of photon emission rates.
  - Plan to add toroidal resolution ⇒
    - \* Can directly simulate fast camera views,
    - \* Quantitative comparison of image intensity,
    - \* Evaluate toroidal spatial averaging.



#### **DEGAS 2 Geometry for C-Mod Shot 1010622**



- Simulations assume steady-state.
  - Compare time scales:
    - \* Autocorrelation time for turbulence =  $10 20 \mu s$ ,
    - \* Time for 3 eV D to travel across cloud = 1  $\mu$ s (2 cm),
    - \* Timescale for emission of  $D_{\alpha}$  photon  $=1/A_{3\rightarrow2}=0.02~\mu\text{s},$
    - \* Note that camera exposure times = 2  $\mu$ s (60 frame/s) or 4  $\mu$ s (5  $\times$  10<sup>6</sup> frames / s),
    - ∗ ⇒ assumption of stationary plasma OK.



#### • Physics:

− D<sub>2</sub>, D<sub>2</sub><sup>+</sup> dissociation, including

\* 
$$e + D_2 \rightarrow e + D(1s) + D(1s)$$
  
\*  $e + D_2 \rightarrow e + D(1s) + D^*(n = 3)$   
\*  $e + D_2 \rightarrow 2e + D_2^+$   
\*  $e + D_2 \rightarrow 2e + D(1s) + D^+$   
\*  $e + D_2^+ \rightarrow 2e + 2D^+$   
\*  $e + D_2^+ \rightarrow e + D(1s) + D^+$   
\*  $e + D_2^+ \rightarrow e + D^+ + D^*(n = 3)$   
\*  $e + D_2^+ \rightarrow D(1s) + D^*(n = 3)$ 

- D + D<sup>+</sup> elastic scattering (i.e., charge exchange),
- $-D_2 + D^+$  elastic scattering,
- e + D ionization,
  - \* "Multi-step", i.e., collisional-radiative model.
- Neutral-neutral collisions not included,
  - \* May not be negligible,
  - \* Need realistic neutral density to treat,
  - \* Can only be computed in 3-D.



– Emission rate ( $m^{-3} s^{-1}$ ) written as:

$$S_{\mathrm{D}_{\alpha}} = \sum_{j=\mathrm{D},\mathrm{D}_{2},\mathrm{D}_{2}^{+}} n_{j} f_{j}(n_{e},T_{e}),$$

\* Where  $n_j =$  ground state atom & molecule density,

$$f_D = \frac{n_D(n=3)}{n_D(n=1)} A_{3\to 2},$$

- $* [n_D(n=3)/n_D(n=1)](n_e,T_e)$  from CR model,
- st Largely determines  $n_e$ ,  $T_e$  dependence of  $f_D$ .

$$f_{D_2}, f_{D_2^+} = n_e \sum_{k} \langle \sigma v \rangle_k(T_e),$$

- \* k = reactions leading to n = 3.
- All puffs are 300 K with cosine distribution,
  - \* Examined sensitivity in preliminary runs,
  - \* Run with  $(\cos \theta)^4$  distribution,
  - \* One with 150 K puff.

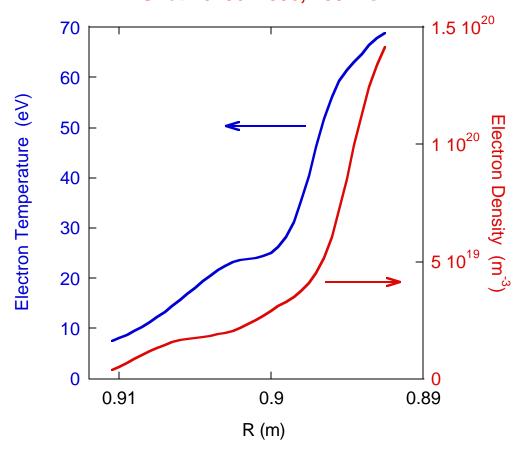


#### • Plasma profiles:

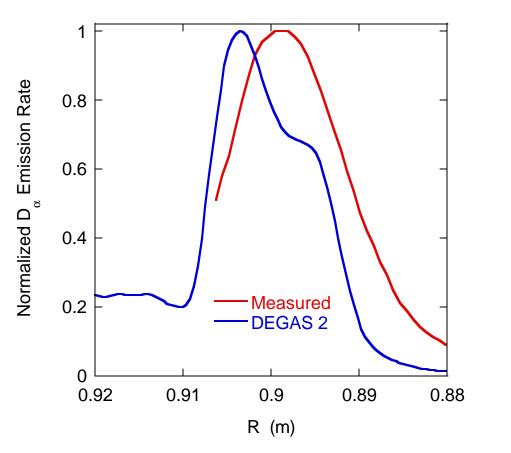
- All are taken from measured data mapped to midplane,
- Assume constant on a flux surface,
  - \* In triangulated region, estimate  $\rho=$  distance between zone center & nearest flux surface mesh zone.
- Assume  $n_i=n_e$ ,  $T_i=T_e$ .



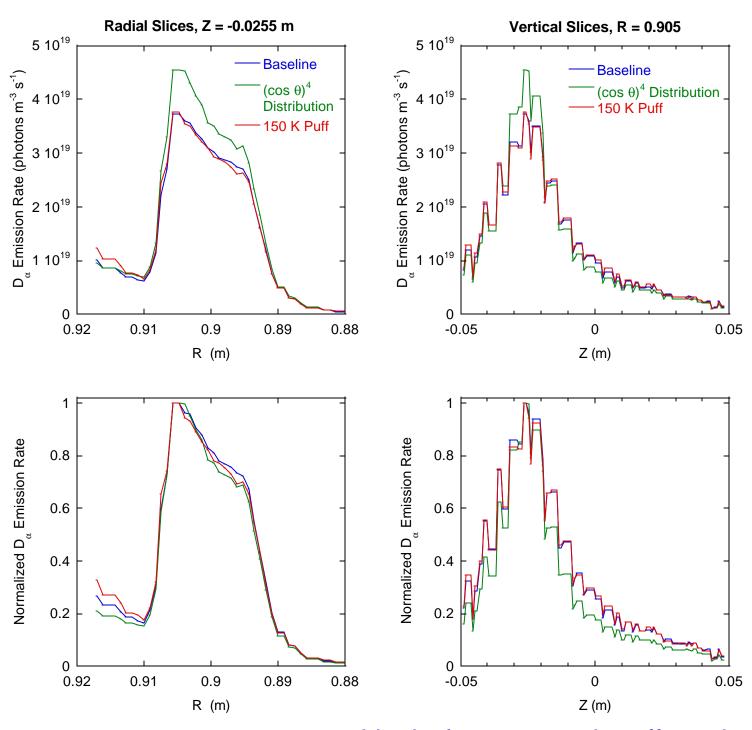
#### Scanning Probe Data from C-Mod Shot 1010622006, 700 ms



Compare DEGAS 2 Result with Experimental Data Radial Slice at Z = -0.034 m



## Peak Location & Width of Simulated Emission Insensitive to Details of D<sub>2</sub> Distribution



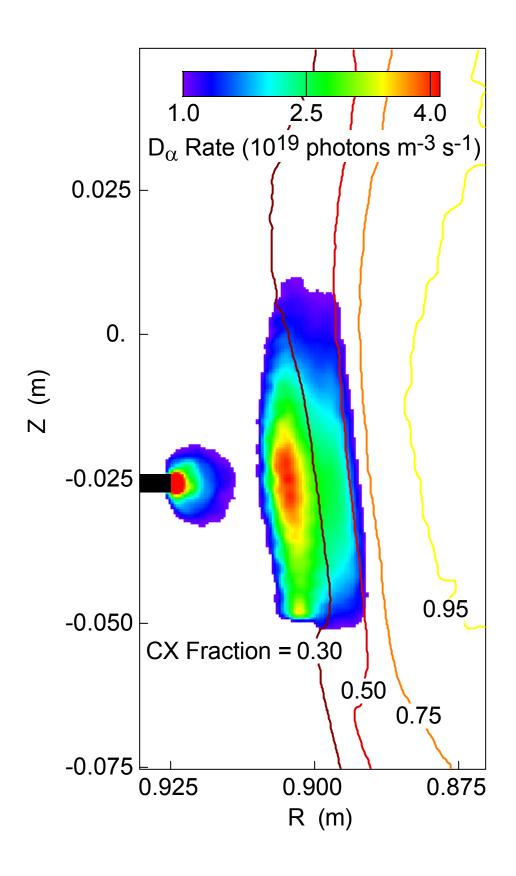
⇒ Vertical extent can be affected

#### **C-MOD RESULTS**

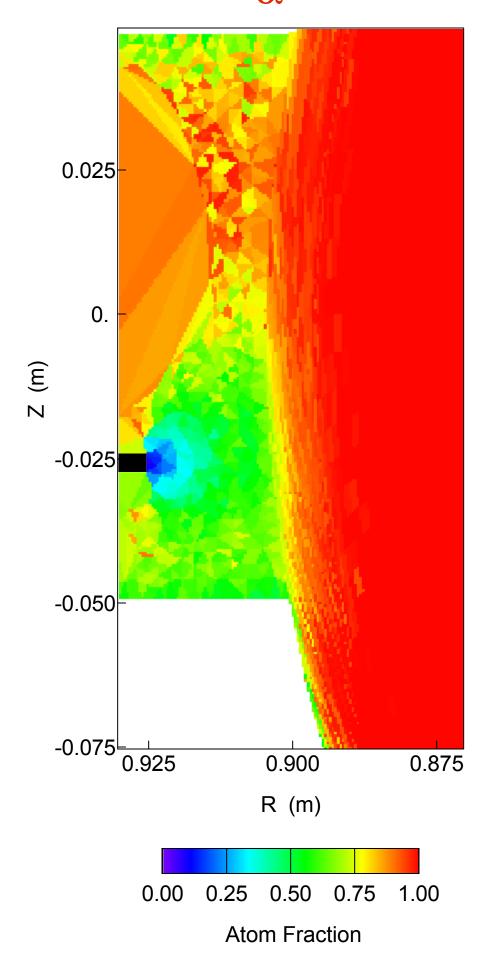
- Alcator C-Mod shot 1010622006 at 700 ms.
- Baseline computed with time-average plasma profiles,
  - -10-20% of atoms in cloud undergone reflection,
  - "CX fraction" have had a CX,
  - Rest from dissociation ⇒ ballistic trajectories.
  - $\Rightarrow \sim 50 -65\%$  of D emission
- At peak, molecular  $D_{\alpha}$ s contribute  $\sim 40\%$ ,
  - < 10% for  $R \lesssim 0.9$  m.
- Compare with time-average experimental GPI images,
  - Emission peak near nozzle not seen experimentally,
  - Probe data assumed constant for R > 0.91 m,
  - Nozzle peak  $\downarrow 10^{-2}$  if  $T_e < 2.5$  eV
  - Or if  $n_e < 3.6 \times 10^{16} \text{ m}^{-3}$ ,
  - Both consistent with exponential extrapolation of probe data.



## **DEGAS 2 Baseline**



## Fraction of $D_{\alpha}$ Due to Atoms



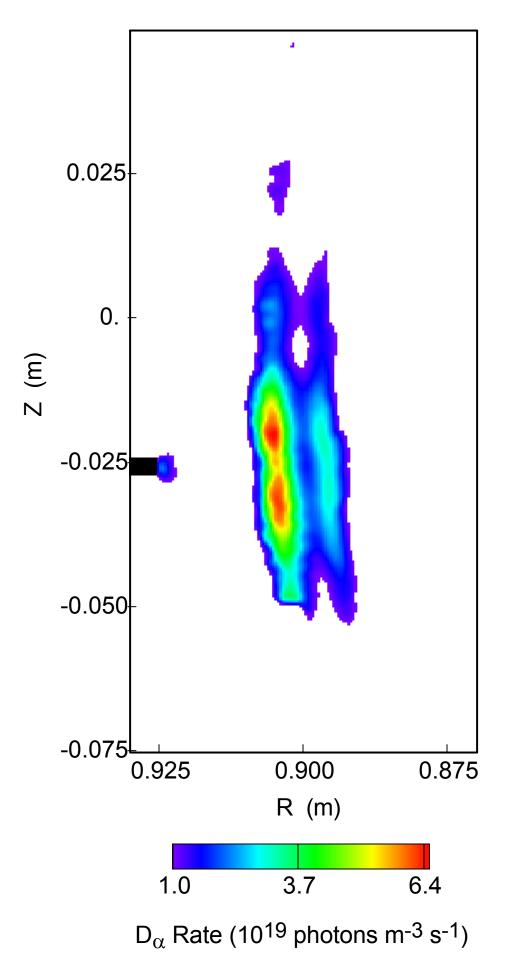
- Impose 2-D perturbation on  $n_e$  and  $T_e$ ,
  - Important to understand relation between spatial variation in emission & underlying plasma fluctuations,
  - Consider ad hoc perturbation:

$$n'_e(R, Z) = n_e(R, Z) \left[1 + \frac{1}{2} \sin(\frac{\pi Z}{0.01})\right] \times \left\{1 + \frac{1}{2} \sin\left[\frac{\pi (R - R_{\text{sep}} + 0.0035)}{0.005}\right]\right\},$$

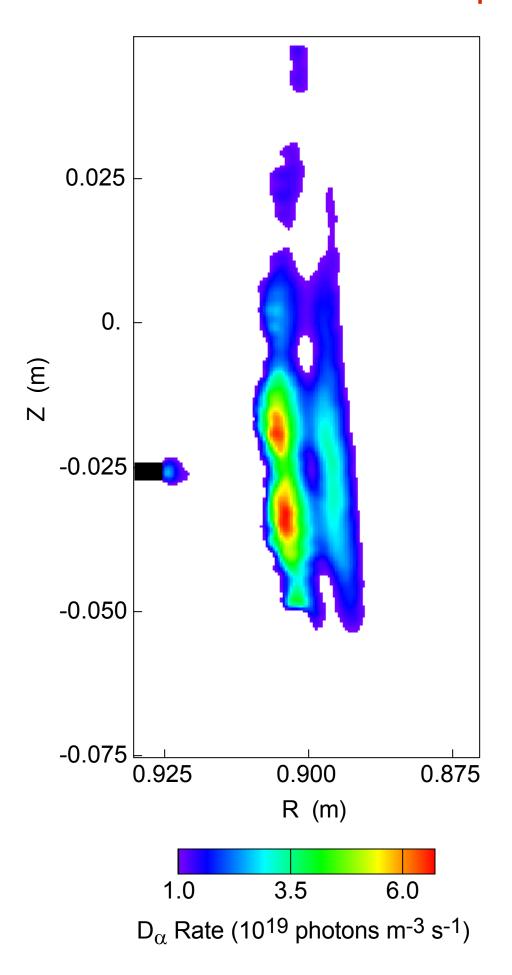
- where:
  - \* The 1/2 factors make this a 50% perturbation,
    - $\cdot$  Factor ranges from 0.25 to 2.25.
  - \* 2 cm wavelength for poloidal ( $\sim Z$ ) variation,
    - Typical size of observed emission structures.
  - \* Used only 1 cm in R because of limited radial width,
    - · 0.0035 shift so innermost data point unchanged.
- Try same perturbation on  $T_e$ ,
  - \* Only difference:  $T_e$  bound between 5 and 100 eV.



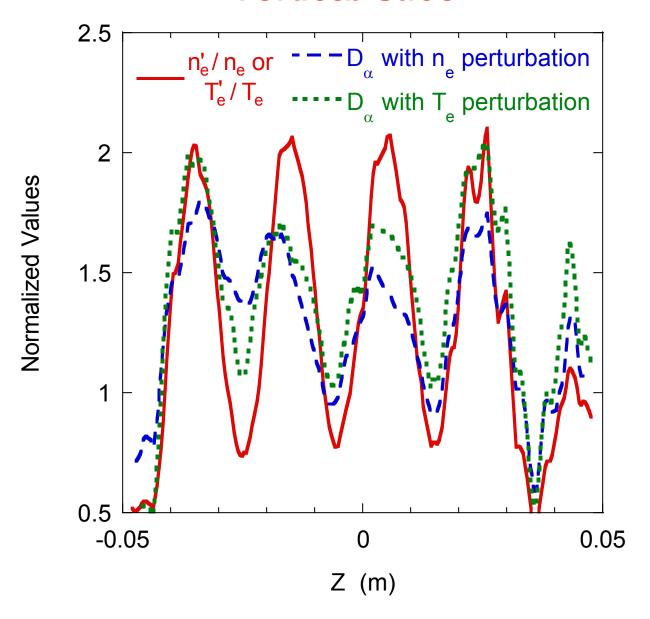
## 2-D Perturbation to Electron Density



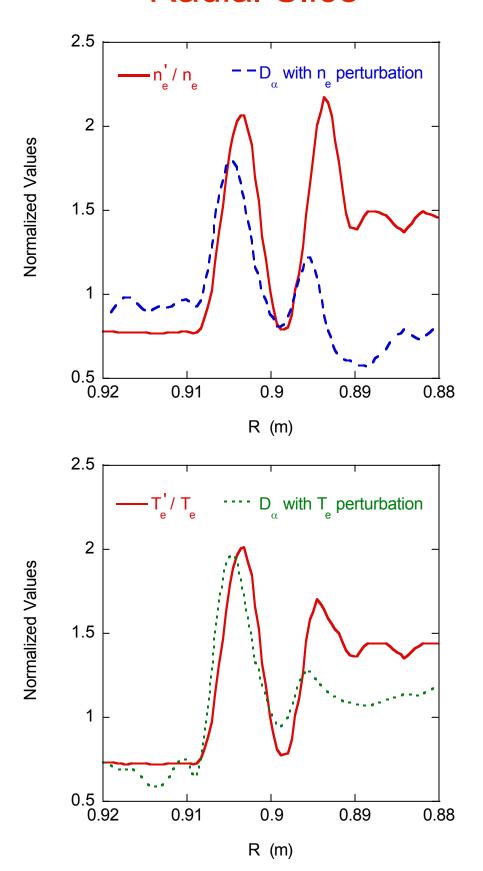
### 2-D Perturbation to Electron Temperature



# Effect of 2-D Perturbation Normalized to Unperturbed Value Vertical Slice



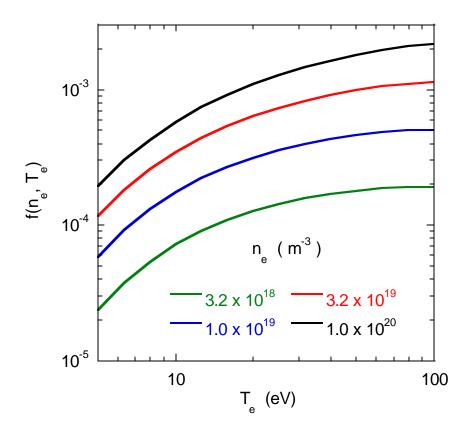
# Effect of 2-D Perturbation Normalized to Unperturbed Value Radial Slice



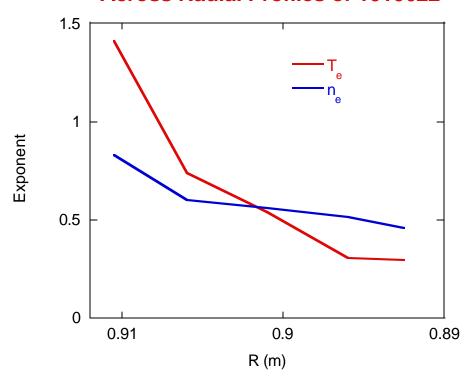
- Both simulations shows same 2-D structure,
- → wavenumber spectrum at least similar to that of plasma turbulence,
  - Expect autocorrelation function
     & frequency spectra similar also,
  - Will subsequently investigate quantitatively.
- Ratio of perturbed / unperturbed emission  $\neq n_e'/n_e$  because  $\partial \ln f_{\rm D}/\partial \ln n_e$ ,  $\partial \ln f_{\rm D}/\partial \ln T_e < 1$ .
- Further complicated by molecular contributions,
  - $*~f_{
    m D_2}$  and  $f_{
    m D_2^+} \propto n_e$ ,
  - \*  $T_e$  dependence not simple,
  - \* Effective scaling varies radially.
- ullet Simple interpretation of GPI: image patterns  $\propto n_e'/n_e$ ,
  - And insensitive to  $T_e$ ,
  - Valid only if  $n_e \lesssim 10^{18}~{\rm m}^{-3}$  and  $T_e \gg 10$  eV,
  - Not the case here!
  - $\Rightarrow n_e$ ,  $T_e$  dependence of  $S_{\mathrm{D}_{\alpha}}$  not different enough to infer perturbation amplitudes,
  - Would be simpler if  $n_e$ ,  $T_e$  in phase.



## $n_e^{}$ , $T_e^{}$ Dependence of $D_a^{}$ Emission Rate Contained in Ratio of n=3 Density to n=1



Scaling of  $f(n_e, T_e)$  Varies Across Radial Profiles of 1010622

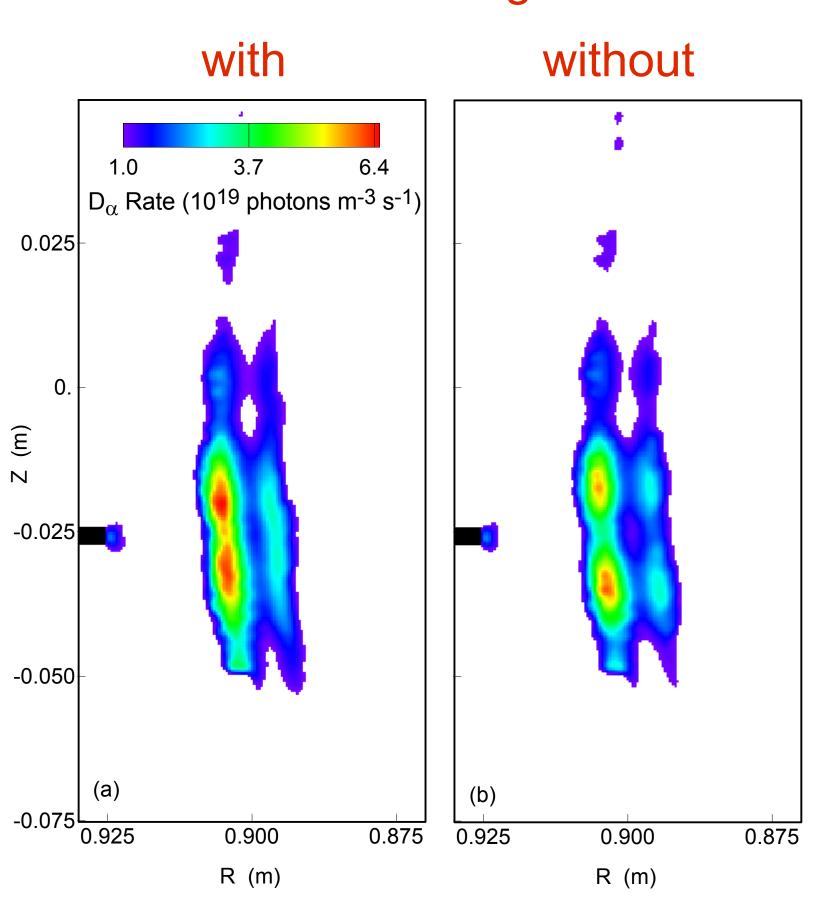


#### **Shadow Fraction**

- Above focussed only on effect of perturbation on  $f_j$ ,
- They also impact  $n_j!$
- "Shadowing effect": ionization caused by local  $n_e$ ,  $T_e$  peak reduces light at smaller R.
- Compare images with and without shadowing,
  - "With" shadowing is as above,
  - To eliminate, use perturbed  $f_i$  and unperturbed  $n_i$ ,
  - "Unshadowed" clearly shows  $n_e$  perturbation structure,
  - Shadowed image smeared out,
    - \* Due to  $n_i$  reductions by  $n_e$  peaks,
    - st And  $n_j$  increases by  $n_e$  minima.



## Runs with Electron Density Perturbation Shadowing:



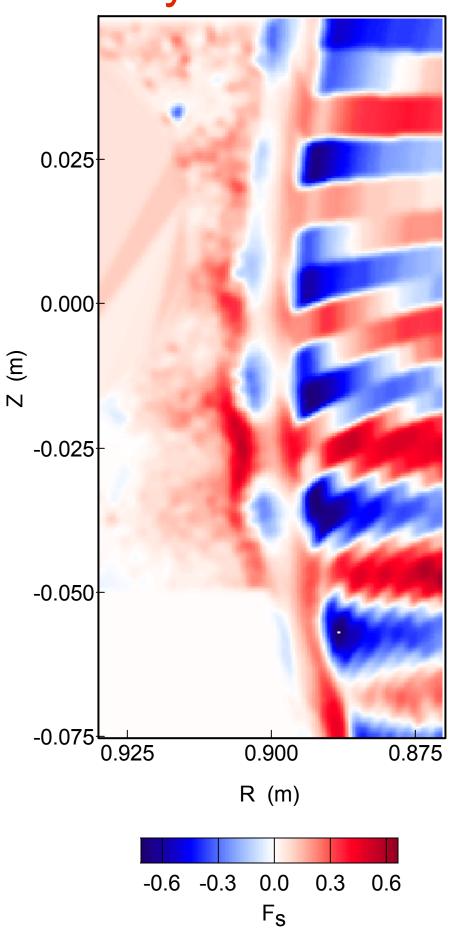
Estimate by computing:

$$F_s = \left[\sum_j (n'_j - n_j)f'_j\right] / \sum_j n_j f_j,$$

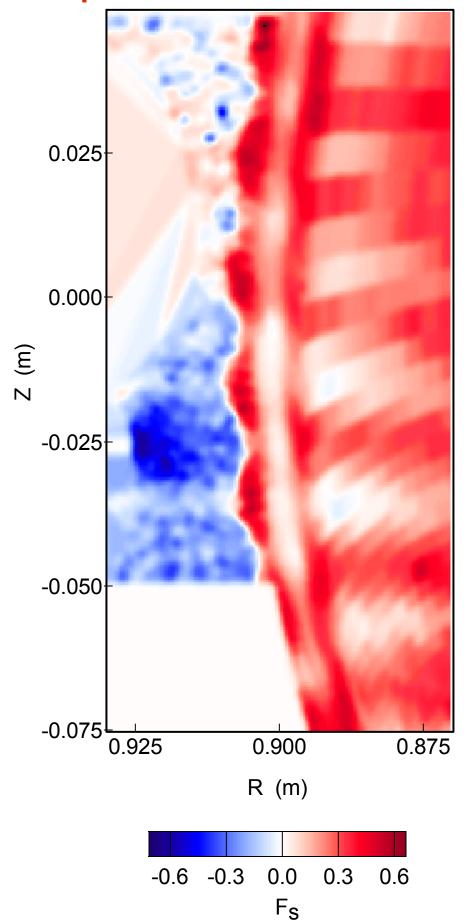
- Where prime indicates perturbed value.
- Evaluate separately for both "perturbed" simulations.
- Structure is complicated!
- Main observations:
  - 1.  $|F_s| \gtrsim 0.5$  in many places  $\Rightarrow$  too large to ignore in GPI analysis.
  - 2. Most of  $F_s$  due to molecules,
    - Analogous quantity based on atoms only  $\leq 0.2$ .
- $\bullet$  To understand  $F_s$  look at radial slices,
  - -Z = -0.034: peak in  $n'_e/n_e$ ,
  - -Z=-0.025: at nozzle & a minimum in  $n_e^\prime/n_e$ .
  - Compare with  $1 n_e'/n_e$ ,
    - \*  $1 n'_e/n_e < 0 \Rightarrow$  local  $n_e >$  unperturbed value,
    - \*  $1 n'_e/n_e > 0 \Rightarrow$  local  $n_e <$  unperturbed value,
    - \*  $T_e$  perturbation differs at edges.
  - $-F_s < 0 \Rightarrow n_i$  locally reduced,
    - \*  $F_s$  drops are in "shadows" of largest  $n'_e/n_e$ .
  - $-F_s > 0 \Rightarrow n_j$  locally increased,
    - \*  $F_s > 0$  at Z = -0.025 since  $n_e$  modulation near min.,
    - \* Not so in perturbed  $T_e$  case due to smaller dissociation rate & strong  $T_e$  dependence of  $f_i$ .



## Shadow Fraction with Density Perturbation

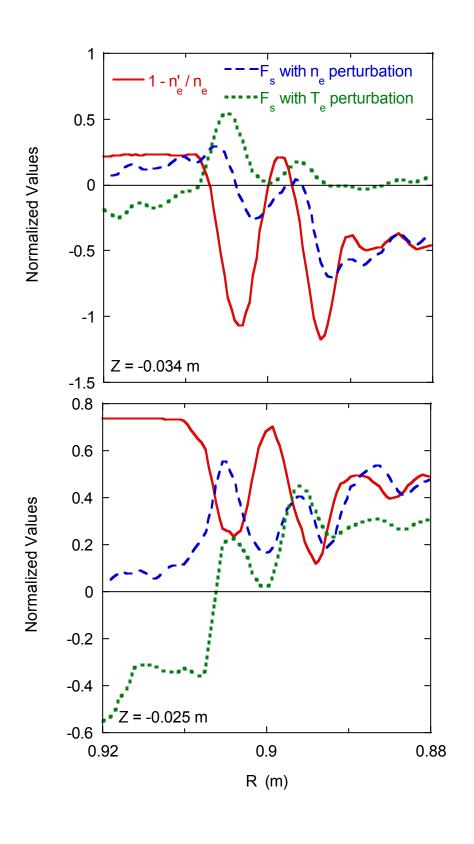


## Shadow Fraction with Temperature Perturbation



#### **Shadow Fraction Significant**

#### Radial Slices



#### **CONCLUSIONS**

- DEGAS 2 simulations show that spatial variation of  $D_{\alpha}$  emission reflects that of  $n_e$ ,  $T_e$  turbulence.
- ullet But,  $n_e$ ,  $T_e$  dependence of emission rate complicated,
  - $\Rightarrow$  no simple scheme to get plasma fluctuations.
- Contributions from molecules significant,
  - Further complicating  $n_e$ ,  $T_e$  dependence,
  - Densities significantly affected by perturbation.
- ⇒ will need neutral transport code to interpret GPI,
  - Must do careful benchmarks first,
  - To verify these conclusions,
  - Validate atomic & molecular physics models.